On the origin of a broad QFP wave train: unwinding jet as the driver

X[inping](http://orcid.org/0000-0001-9374-4380) Zhou $\Phi, ^{1,2}$ Z[ehao](http://orcid.org/0000-0003-0880-9616) Tang $\Phi, ^{3}$ Z[hining](http://orcid.org/0000-0001-8318-8747) Qu $\Phi, ^{1}$ [K](http://orcid.org/0000-0002-1134-4023)e Yu $\Phi, ^{1}$ C[hengrui](http://orcid.org/0009-0005-5300-769X) Zhou $\Phi, ^{3}$ Yuqi Xiang, 1 Ahmed Ahmed I[brahim](http://orcid.org/0000-0001-9540-5235) $\Phi, ^{4}$ and YUANDENG SHEN ^(D)

¹ *College of Physics and Electronic Engineering, Sichuan Normal University, Chengdu 610068, People's Republic of China* ²*State Key Laboratory of Space Weather, Chinese Academy of Sciences, Beijing 100190*

³*Yunnan Observatories, Chinese Academy of Sciences, Kunming 650216, People's Republic of China*

⁴*Department of Physics and Astronomy, College of Science, King Saud University, P.O. Box 2455, 11451 Riyadh, Saudi Arabia*

⁵*Shenzhen Key Laboratory of Numerical Prediction for Space Storm, School of Aerospace, Harbin Institute of Technology, Shenzhen 518055, China*

ABSTRACT

Large-scale extreme-ultraviolet (EUV) waves commonly exhibit as single wavefront and are believed to be caused by coronal mass ejections (CMEs). Utilizing high spatiotemporal resolution imaging observations from the Solar Dynamics Observatory, we present two sequentially generated wave trains originating from the same active region: a narrow quasiperiodic fast-propagating (QFP) wave train that propagates along the coronal loop system above the jet and a broad QFP wave train that travels along the solar surface beneath the jet. The measurements indicate that the narrow QFP wave train and the accompanying flare's quasiperiodic pulsations (QPPs) have nearly identical onsets and periods. This result suggests that the accompanying flare process excites the observed narrow QFP wave train. However, the broad QFP wave train starts approximately 2 minutes before the QPPs of the flare, but consistent with the interaction between the unwinding jet and the solar surface. Moreover, we find that the period of the broad QFP wave train, approximately 130 s, closely matches that of the unwinding jet. This period is significantly longer than the 30 s period of the accompanying flare's QPPs. Based on these findings, we propose that the intermittent energy release of the accompanying flare excited the narrow QFP wave train confined propagating in the coronal loop system. The unwinding jet, rather than the intermittent energy release in the accompanying flare, triggered the broad QFP wave train propagating along the solar surface.

Keywords: Solar coronal waves(1995) — Alfvén waves (23) — Solar corona (1483)

1. INTRODUCTION

Hydromagnetics waves, as a fundamental physical phenomenon, can be utilized to infer the physical parameters of the medium they propagate. Consequently, they offer a mean to diagnose coronal physical parameters, such as magnetic field strength, utilizing seismological diagnostic techniques [\(Uchida](#page-9-0) [1970;](#page-9-0) [Roberts et al.](#page-9-1) [1984\)](#page-9-1), and provide a possibility to explore the plasma density, temperature, as well as magnetic field strength inside the coronal hole using the lensing effect of the waves [\(Zhou et al.](#page-10-0) [2024b,](#page-10-0) [2022c\)](#page-10-1).

In the last half-century, large-scale extreme ultraviolet (EUV) waves have attracted many researchers to investigate them [\(Thompson et al.](#page-9-2) [1998\)](#page-9-2). Their physical nature and driven mechanism have finally been unified after many years of debate, namely, they are a fast-mode magnetosonic wave driven by the lateral expansion of the accompanying coronal mass ejections (CMEs) [\(Wu et al.](#page-9-3) [2001;](#page-9-3) [Chen et al.](#page-8-0) [2002;](#page-8-0) [Ma et al.](#page-9-4) [2011;](#page-9-4) [Li et al.](#page-9-5) [2012;](#page-9-5) [Liu et al.](#page-9-6) [2018,](#page-9-6) [2019;](#page-9-7) [Mei et al.](#page-9-8) [2020;](#page-9-8) [Hou et al.](#page-8-1) [2022;](#page-8-1) [Chen](#page-8-2) [2023a\)](#page-8-2). It is important to note that small-scale EUV waves, which are not associated with CMEs, have also been observed. However, these waves's sizes are relatively small, and the number of observations is limited. For instance, the small-scale EUV wave triggered by breakout reconnection in the fan-spine topology has been documented [\(Kumar et al.](#page-8-3) [2016\)](#page-8-3). [Shen et al.](#page-9-9) [\(2017,](#page-9-9)

Corresponding author: Xinping Zhou [xpzhou@sicnu.edu.cn](mailto: xpzhou@sicnu.edu.cn)

Corresponding author: Yuandeng Shen [ydshen@hit.edu.cn](mailto: ydshen@hit.edu.cn)

[2018d,](#page-9-10)[c\)](#page-9-11) and [Zheng et al.](#page-10-2) [\(2020\)](#page-10-2) found that the waves can be driven by the fast expansion of the lower coronal loops associated with the failed filament eruption or by the impingement of the associated coronal jets. Additionally, [Liu et al.](#page-9-12) [\(2023\)](#page-9-12) proposed that the expansion of the newly formed loops can also be one of the driving sources of the small-scale EUV wave, resembling the slingshot mechanism in the eruption of the coronal jets [\(Su et al.](#page-9-13) [2015;](#page-9-13) [Antolin et al.](#page-7-0) [2021\)](#page-7-0). At the same time, some researchers find that the small-scale EUV waves can be directly driven by the ejection of a blowout surge or jet [\(Zheng et al.](#page-10-3) [2012,](#page-10-3) [2013;](#page-10-4) [Chen et al.](#page-7-1) [2021;](#page-7-1) [Hou et al.](#page-8-4) [2023\)](#page-8-4). As pointed out by [Shen et al.](#page-9-10) [\(2018d\)](#page-9-10), the small-scale EUV wave driven by the sudden loop expansion, the surges or jets have a shorter lifetime than those with typical hour-long lifetime excited by the CMEs (see the reviews [Liu & Ofman](#page-9-14) [2014;](#page-9-14) [Warmuth](#page-9-15) [2015,](#page-9-15) and references therein). For convenience, the large- and small-scale EUV waves are collectively referred to as classical EUV waves.

In the past, the classical EUV waves were consistently perceived as a single-pulse phenomenon, resulting in little attention being paid to their possible periodicities. Recently, two new types of EUV wave trains with multiple wavefronts, captured by Atmosphere Imaging Assembly (AIA; [Lemen et al.](#page-8-5) [2012\)](#page-8-5) onboard the Solar Dynamics Observatory (SDO; [Pesnell et al.](#page-9-16) [2012\)](#page-9-16), have rekindled interest in the study of the EUV wave, these are, narrow [\(Liu et al.](#page-9-17) [2011;](#page-9-17) [Shen & Liu](#page-9-18) [2012;](#page-9-18) [Yuan et al.](#page-10-5) [2013;](#page-10-5) [Zhou](#page-10-6) [et al.](#page-10-6) [2022a\)](#page-10-6) and broad [\(Liu et al.](#page-9-19) [2012;](#page-9-19) [Kumar et al.](#page-8-6) [2017;](#page-8-6) [Shen et al.](#page-9-20) [2019;](#page-9-20) [Zhou et al.](#page-10-7) [2021,](#page-10-7) [2022b,](#page-10-8)[c,](#page-10-1) [2024a\)](#page-10-9) quasiperiodic fast-propagating (QFP) wave trains, albeit only in sporadic cases. For detailed information regarding their respective features, please refer to Table 1 of the review article by [Shen et al.](#page-9-21) [\(2022\)](#page-9-21). The significant difference between them and the classical EUV waves is that these two types of waves have multiple wavefronts. The narrow QFP wave train, first reported by [Liu et al.](#page-9-17) [\(2011\)](#page-9-17), propagates along the coronal loops system with a speed ranging from 300 km s⁻¹ to 2400 km s⁻¹ in a confined manner [\(Liu & Ofman](#page-9-14) [2014;](#page-9-14) [Shen et al.](#page-9-21) [2022\)](#page-9-21). Generally, they are believed to be triggered by the intermittent energy release in the accompanying flare [\(Liu et al.](#page-9-17) [2011;](#page-9-17) [Shen & Liu](#page-9-18) [2012;](#page-9-18) [Zhou et al.](#page-10-6) [2022a\)](#page-10-6). The broad QFP wave train, similar to the classical EUV wave propagating along the solar surface, will display the refraction, transmission as well as total reflection when they interact with various coronal structures, such as filaments, coronal loops, and coronal holes [\(Liu et al.](#page-9-19) [2012;](#page-9-19) [Shen et al.](#page-9-20) [2019;](#page-9-20) [Zhou et al.](#page-10-8) [2022b,](#page-10-8)[c,](#page-10-1) [2024c\)](#page-10-10). Notably, utilizing the theoretical results by [Piantschitsch & Terradas](#page-9-22) [\(2021\)](#page-9-22), [Zhou et al.](#page-10-8) [\(2022b\)](#page-10-8) first certified a broad QFP wave train *total reflected* from the boundary of a south coronal hole, marking the last piece of the puzzle of the properties of the true wave to be found. According to the statistic by [Shen et al.](#page-9-21) [\(2022\)](#page-9-21), the speed of the broad wave train is in the range of 370-1100 km s⁻¹, which is consistent with that of the classical EUV with a speed of 200-1500 km s⁻¹. Although many characteristics of the broad QFP wave train, as mentioned above, are similar to the classical EUV wave, the driven mechanism for the latter is hardly used to explain the formation of the broad QFP wave train. The main reason is that it is difficult for a single energy-releasing process, such as the eruption CME, to stimulate the wave train with multiple wavefronts. There are different insights into the trigger mechanisms of the few observed broad QFP waves. For example, [Sun et al.](#page-9-23) [\(2022\)](#page-9-23) believe that the broad wave train might be triggered by the successive stretching of the magnetic field lines during the solar eruption, where the speed ratio of the inner edge of the wave train and the wave train is approximately one-third. Their results align with the simulation's expectations by [Chen et al.](#page-8-0) [\(2002\)](#page-8-0). [Wang et al.](#page-9-24) [\(2021\)](#page-9-24) reproduced the broad QFP wave train with a dome shape propagating perpendicular to the magnetic field lines with a speed of about 550-700 km s⁻¹ associated with a failed filament eruption. Their result indicates that CME is not necessarily involved in broad QFP wave train excitation. This finding has been certified from the observation view. For instance, [Zhou et al.](#page-10-8) [\(2022b\)](#page-10-8) and [Zhou et al.](#page-10-1) [\(2022c\)](#page-10-1) found that the broad QFP wave train share a common period with the associated flare. Thus, they propose that the nonlinear energy release processes in the accompanying flare should drive this QFP wave. Although the discovery of these two types of waves enriches the observation feature of the coronal wave, it also implies that the triggering mechanism of the EUV wave is still an open question. Notability, sometimes classical EUV waves can be captured when they encounter the coronal loops system, resulting in these waves propagate inside it [\(Zhou et al.](#page-10-7) [2021;](#page-10-7) [Li et al.](#page-8-7) [2024c\)](#page-8-7). In this process, the wave speed will be significantly increased due to the wave mode conversion [\(Chen](#page-8-8) [2016;](#page-8-8) [Chandra et al.](#page-7-2) [2018;](#page-7-2) [Kumar et al.](#page-8-9) [2024\)](#page-8-9). Unfortunately, there is no observational evidence yet of broad QFP wave train being captured by coronal loops.

In this letter, we report, for the first time, the direct observational evidence of the broad QFP wave train driven by the unwinding jet utilizing the SDO/AIA high spatiotemporal resolution imaging data. In contrast, the intermittent energy release of the accompanying flare triggered the narrow QFP wave train. The layout of the remaining paper is as follows: Section [2](#page-1-0) gives the observational analysis and results; Section [3](#page-4-0) presents the discussion and conclusion.

2. RESULTS

2.1. *The unwinding jet*

The event occurred close to the western disk limb of the NOAA AR 11149 on 2011 January 27, associated with a B6.6 class flare, whose start, peak, and end time were 08:40 UT, 08:50 UT, and 08:53 UT, respectively. An overview of the eruption source

region dominated with some open loops, highlighted with the green extrapolated magnetic field lines, using the Potential Field Source (PFSS; [Schrijver & De Rosa](#page-9-25) [2003\)](#page-9-25) mode, is presented in Figure [1](#page-5-0) (a). Under the loops system, a mini filament lay prone under it. The snapshots in Figure [1](#page-5-0) (b)-(i) show the evolution of the jet using AIA 304 Å and 131 Å raw images. This jet displays a straightforward evolution process in the plane of the sky, which is advantageous for conducting a detailed study of its rotation process. From the animation of Figure [1,](#page-5-0) one can find that the jet started at about 08:35 UT and ended at about 08:55 UT, exhibiting apparent rotation motions around the jet's center axis, during its rising period. Beginning from 08:38 UT, the jet is started to unwind, and its body became brighter, marked with the white arrows in Figure [1](#page-5-0) (e) and (h). During the initial phase, the jet developed into a long cylindrical shape with many helical bright plasmas on its surface (see Figure [1](#page-5-0) (c)-(f)). Subsequently, as the whole helical body was rising higher, the jet displayed a highlight untwist magnetic field lines (see Figure [1](#page-5-0) (f)). For more details of the jet's evolution process, please refer to the animation of Figure [1.](#page-5-0)

Upon comparing observation of the jet from the AIA 304 Å channel with it from 131 Å channel observations, one can note that AIA 131 Å channel images had a more simple bright structure along the line-of-sight. It facilitates us to use them to track the jet's rotation process. To reveal the kinematics of the jet more clearly, we established a coordinate system *x* ′ − *y* ′ with its *y* ′−axis along the jet's center axis to track the rotation motion, as shown in Figure [1](#page-5-0) (g). Its origin coordinate *o'*, [*a*, *b*], is [937, 228], and the rotation angle, θ , is $-(0.93 + \pi/2)$ $-(0.93 + \pi/2)$ $-(0.93 + \pi/2)$. Figure 2 (a1) shows the relative position of the coordinate system *x'* − *y'*, with a retation angle θ to the solar arcsec *x* − *y* coordinate system. We track a specif rotation angle θ , to the solar arcsec *x* − *y* coordinate system. We track a specific moving bright feature (MBF, whose location has been marked by a white arrow in panel AIA 131 Å of the animation of Figure [1\)](#page-5-0) during 08:42:08 UT−08:43:20 UT in the solar arcsec coordinate system $x - y$. Their locations relative to the $x' - y'$ coordinate system, transformed using Equations [1](#page-2-0) and [2,](#page-2-1) are overlaid on it marked with "+" in the inset of Figure [2](#page-6-0) (a1).

$$
\begin{cases}\n x = a + x' \cos \theta - y' \sin \theta \\
y = b + x' \sin \theta + y' \cos \theta\n\end{cases}
$$
\n(1)

$$
\begin{cases}\n x' = y \sin \theta - b \sin \theta - a \cos \theta + x \cos \theta \\
y' = a \sin \theta - x \sin \theta + y \cos \theta - b \cos \theta\n\end{cases}
$$
\n(2)

Based on the coordinates in the $x' - y'$ coordinate system, we present the temporal evolution of the x' – and y' –components in Figure [2](#page-6-0) (a2) and (a3), respectively. By analyzing the distributions of these two components, we can easily find that the motion of the MBF exhibits a spiral pattern around the *y'*−axis, i.e., the jet's center axis. To characterize this motion, we fit a cosine function, $x' = r\sin(\frac{2\pi}{T}(t-\sigma))$, to the transverse motion in the *x'* direction, assuming that the radius of the jet dose not change
during selected period, and a linear function to the radial motion in the *y'* direction during selected period, and a linear function to the radial motion in the *y'* direction. Our fitting yields the following parameters for the jet: a period of *T* = 120 ± 8 s, an angular speed of $\omega = 0.052$ rad s⁻¹ (or 3° s⁻¹), a rotation radius of *r* = 6.5 ± 0.4 Mm, a
linear velocity of $v_0 = 340 \pm 12$ km s⁻¹, and a radial speed of $v_0 = 375 \pm$ linear velocity of $v_l = 340 \pm 12$ km s⁻¹, and a radial speed of $v_r = 375 \pm 15$ km s⁻¹. Also, we select five cuts, marked with S1-S5 in Figure [1](#page-5-0) (c), to study the kinematic of the jet in the transverse and radial directions, and the relevant time-distance stack plots are displayed in Figure [2.](#page-6-0) Consequently, the speed of the helical structure is in the range of 150-160 km s⁻¹ through fitting the bright stripes on the time-distance stack plots using a linear function (see Figure [2](#page-6-0) (b1)-(c3)), while its radial speed is 405 ± 23 km s^{−1} (see Figure [2](#page-6-0) (d)). Compared with these two methods mentioned above, we can find that the obtained radial speeds are similar, 375 km s⁻¹ and 405 km s⁻¹, while the transverse speeds have a relatively significant difference, 340 km s⁻¹ and 150 km s⁻¹. The disparity in transverse speeds is reasonable given that it derived from the time-distance stack plots represent projection speeds on the sky plane and do not consider the movement of the MBF along the surface of the cylindrical jet. Additionally, the diameter of the jet has shown a substantial increase from approximately 14 Mm to 22 Mm (refer to Figure [2](#page-6-0) (b2)). It suggests that the jet experienced significant expansion during its eruption. It is important to note that this expansion phenomenon is exclusive to the side far to the solar surface. Conversely, on the side closer to the solar surface, the column plasma density of the jet has exhibited a considerable rise compared to that observed on the sides away from the solar surface, which can be verified by the obvious difference brightness between them in Figure [2](#page-6-0) (b1)-(c3). This column plasma density disparity on both side of the jet can be attributed to the mutual compression between the jet and the solar surface.

2.2. *Kinematics of the QFP wave trains*

Here, we mainly analyze the time sequence of the AIA 171 Å, 193 Å, and 211 Å running-difference images to the overall evolutionary process of the wave trains. In the technique of running difference, each image in a sequence of images is subtracted from the previous 12 s image to enhance moving features. As shown in Figure [3,](#page-7-3) during the violent eruption launched two different wave trains: multiple successive wavefronts with an angle about 15°, observed from the perspective of the SDO, propagating

4 Zhou et al.

along the solar limb, others, with an angle about 5° running along the funnel-like open-loops system.^{[1](#page-3-0)} These two wave trains are marked with red and green arrows in Figure [3,](#page-7-3) respectively. The images demonstrate the presence of the broad wave train, which, much like the classical EUV wave, is prominently visible in 171 Å, 193 Å, and 211 Å channels, with a particularly distinct appearance in the 193 Å and 211 Å channels. On the other hand, the narrow wave train is solely observable in the AIA 171 Å channel. These characteristics are consistent with previous reports about them [\(Liu et al.](#page-9-17) [2011;](#page-9-17) [Shen & Liu](#page-9-18) [2012;](#page-9-18) [Zhou et al.](#page-10-6) [2022a,](#page-10-6)[b,](#page-10-8)[c\)](#page-10-1). Particularly, the first wavefront of the broad wave train appears much longer than the following ones because the unwinding motion is a spatially widening spiral, resulting in the front part of the jet compressing the plasma more pronounced on the side near the solar surface. In this process, the closer to the solar surface side, the more pronounced the jet squeezing of the solar atmosphere, which results in the intensity of the wavefront becoming progressively stronger as it approaches the solar surface. This can be verified from Figure 3 (e) and (f). Additionally, the fact that the second and third wavefronts are weaker than the first one leads to their length of manifestation appearing to be much shorter than that of the leading wavefront. It is noteworthy that the narrow QFP wave became pronounced since 08:45:08 UT near the flare kernel, However, the amplitude is smaller than that after 08:46:44 UT. The broad QFP wave was observed at a considerable distance of approximately 100 Mm, initiated at 08:44:56 UT (see the animation of Figure [3\)](#page-7-3). Notably, we obtained the same QFP structures after increasing the time resolution for reconstructing running-difference images from 12 s up to 24 s and 36 s, indicating that the wave signal was not affected by the stroboscopic effect.

To analyze the kinematics of the broad and narrow wave trains, we reconstructed the time-distance stack plots using the AIA 171 Å and 193 Å running-difference images along the paths Sa and Sb shown in Figure [3](#page-7-3) (d). The time-distance stack plots are displayed in Figure [4](#page-8-10) (a1)-(a3), in which one can find that there exist multiple wavefronts with a speed of 370 ± 16 km s⁻¹ and an acceleration -0.43±0.01 km s⁻². It is worth noting that the wavefronts gradually become diffuse after propagating about 70 Mm in the AIA 171 Å channel (as shown in Figure [4](#page-8-10) (a1)), resulting in wavefronts features that are increasingly difficult to be distinguished. This phenomenon is similar to the classical EUV wave that is best seen in 193 Å and 211 Å channels [\(Liu &](#page-9-14) [Ofman](#page-9-14) [2014\)](#page-9-14). In contrast to the broad QFP wave train propagating along the solar limb, the observed narrow QFP wave train confined in the loops system and only to be observed in 171 Å channel, propagated with a higher speed of over 1000 km s^{-1} (see Figure [4](#page-8-10) (a3)), which is consistent with that reported by previous researchers [\(Shen et al.](#page-9-26) [2018b;](#page-9-26) [Miao et al.](#page-9-27) [2021;](#page-9-27) [Zhou et al.](#page-10-8) [2022b\)](#page-10-8). The speed and acceleration of the broad QFP wave train propagating along the solar limb are in the range of the classical EUV wave [\(Nitta et al.](#page-9-28) [2013\)](#page-9-28), but significantly lower than that of the narrow wave train (dominate speed is over 1000 km s[−]¹ as reported by [Shen et al.](#page-9-21) [\(2022\)](#page-9-21)). These features indicate that the broad wave train present here, similar to that reported by [Zhou](#page-10-8) [et al.](#page-10-8) [\(2022b](#page-10-8)[,c\)](#page-10-1), is a rare broad QFP wave train.

The quasiperiodic pulsations (QPPs) can be responsive to the quasiperiodic energy release process (Nakariakov $\&$ Stepanov [2007;](#page-9-29) [Nakariakov & Melnikov](#page-9-30) [2009;](#page-9-30) [Li et al.](#page-8-11) [2020a;](#page-8-11) [Li & Chen](#page-8-12) [2022;](#page-8-12) [Zhang](#page-10-11) [2024\)](#page-10-11), which have the potential to trigger either a narrow wave train [\(Liu et al.](#page-9-17) [2011;](#page-9-17) [Shen & Liu](#page-9-18) [2012;](#page-9-18) [Zhou et al.](#page-10-6) [2022a\)](#page-10-6) or broad wave train [\(Zhou et al.](#page-10-7) [2021,](#page-10-7) [2022c,](#page-10-1)[b\)](#page-10-8), via magnetic reconnection. Comparing the AIA 9[4](#page-8-10) Å, 131Å and 335 Å light curves in Figure 4 (b1) measured from the flaring kernel region (see the black box in Figure [1](#page-5-0) (i)), one can find that they have a similar trend with the GOES 1-8 Å flux (with an impulsive phase about 8:41 UT to 8:51 UT, see Figure [4](#page-8-10) (b2)), suggesting that no violent eruption in other regions during the present event. According to the Neupert effect [\(Neupert](#page-9-31) [1968;](#page-9-31) [Li et al.](#page-8-13) [2024a\)](#page-8-13), the time-derivative of soft X-ray fluxes can be viewed as a proxy of the corresponding hard X-ray fluxes that reflects the variation of non-thermal particles accelerated by the magnetic reconnection in flares. The detrend time-derivative of GOES 1-8 Å flux obtained from the intensity profile by subtracting its smoothed intensity profile with 60 s boxcar, which enhances periods shorter than 60 s, thus highlighting short-period periodicity features in the wavelet spectrum [\(Kupriyanova et al.](#page-8-14) [2013;](#page-8-14) [Li et al.](#page-9-32) [2021\)](#page-9-32). Additionally, the time cadence of the GOES data is 2 s. Therefore, the GOES data is suitable for detecting the periods of the flare QPPs longer than 6 seconds with the wavelet analysis (Torrence $&$ Compo [1998\)](#page-9-33) that has been widely utilized to analyze the periodicity of time-dependent one-dimensional data [\(Zhang et al.](#page-10-12) [2015,](#page-10-12) [2016;](#page-10-13) [Li & Zhang](#page-9-34) [2017;](#page-9-34) [Li et al.](#page-9-35) [2018,](#page-9-35) [2020c](#page-9-36)[,b;](#page-8-15) [Zhang et al.](#page-10-14) [2022;](#page-10-14) [Li et al.](#page-8-16) [2024b\)](#page-8-16). Using the detrend time-derivative of GOES 1-8 Å flux as input and selecting the Morlet function as the mother function, the wavelet spectrum shows that the flare period is about 30 ± 4 30 ± 4 s, as shown in Figure 4 (c1). To reveal the period of the broad QFP wave train, we extracted the intensity profile at the positions marked with white arrows in Figure [4](#page-8-10) (a2), and the wavelet spectrum is shown in Figure [4](#page-8-10) (c2). Clearly, the main periods of the broad QFP wave train was about 130 ± 25 s. For the broad QFP wave train, the smoothing time window width used here is 4×60 s. We get a similar result when using 0.4×60 s, 1×60 s, 2×60 s, 3×60 s as the smoothing time window width, indicating the period of the broad QFP wave not an artifact of the smoothing procedure. We

¹ According to the statistics by [\(Shen et al.](#page-9-21) [2022\)](#page-9-21), the typically angular width of the narrow and broad QFP wavefront are in the range of $8°-80°$ and $90°-360°$, respectively. The angular width, 15°, of broad QFP wavefronts present here significantly out its typical range. That is due to the affect of projection effect, resulting only observing part of the wavefront from the view of SDO.

also check the periods of the broad QFP wave by another method: The red line in Figure [4](#page-8-10) (a2) marks the duration of the three wavefronts, which is about 7 minutes. Therefore, we can get its period to be about $7 \times 60 \div 3 = 140$ s. This result is similar to that obtained from the wavelet analysis, indicating that the wavelet analysis should be reliable. Combining the animation of Figure [3](#page-7-3) and the time-distance stack plot of the narrow QFP wave train displayed in Figure [4](#page-8-10) (a3), we can find that the frequency of the narrow QFP wave train was significantly high than that of the broad QFP wave. In Figure [4](#page-8-10) (d1)-(d3), we can see that a wavefront appeared at the red arrow position at 08:46:58 UT, 12 s later, at 08:47:00 UT the dimming region followed the wavefront reached the red arrow position. Then, at 08:47:12 UT, the second wavefront appeared at the red arrow position. Therefore, we can infer that the period of the narrow QFP wave train is about 24 s, which is in good agreement with that of the flare QPPs. However, we are not able to prove this period using the wavelet analysis because of the low time resolution (12 s) of the SDO data. The period of the broad wave train is much larger than that of the flare' QPPs but shares a common period, about 2 minutes, with that of the unwinding jet. The close period relationship between the unwinding jet and the broad QFP wave train suggests that the broad QFP wave train should have a tight connection with the successive expansion and untwist of the rotation jet. Additionally, according to the statistics by [Shen et al.](#page-9-21) [\(2022\)](#page-9-21), the broad QFP wave train is always associated with the flare class exceeding the C-class. This correlation arises from the higher energy threshold required to trigger a broad wave train compared to a narrow wave train, leading to the fact that the B-class flare reported here can not trigger the broad wave train instead of the narrow wave train. This result is supported by the fact that the energy flux density of the broad wave train is typically higher than that of the narrow wave train, as indicated in the statistics by [Shen et al.](#page-9-21) [\(2022\)](#page-9-21) (where the energy flux density of the broad and narrow waves ranges from 10-19 × 10⁵ erg cm⁻² s⁻¹ and 0.1-4 × 10⁵ erg cm⁻² s⁻¹, respectively). For the narrow QFP wave train, we believe that, as the previous results [\(Liu et al.](#page-9-17) [2011;](#page-9-17) [Shen & Liu](#page-9-18) [2012\)](#page-9-18), the flare's QPPs is their driving source due to the close temporal and period relationship between this two.

3. DISCUSSION AND CONCLUSIONS

In this work, we studied the simultaneous appearance of two scarce QFP wave trains, each characterized by multiple wavefronts. The event associated with a unwinding jet eruption on 2011 January 27. The broad QFP wave train was observed to propagate along the solar disk limb at a speed of 370±16 km s⁻¹. In contrast, the narrow QFP wave train, confined within a funnel-shaped loops-system that overlaid the jet, propagated with a speed of 1040±60 km s⁻¹. Upon analyzing the measured parameters, our result suggests that the broad QFP wave train reported here is not predominantly associated with flare QPPs; instead, it appears to be triggered by an unwinding jet, contrary to earlier studies. On the contrary, the released energy behind the flare QPPs excited the narrow QFP wave train.

To date, the number of observed broad QFP wave events is quite limited, with up to 8 such events identified. A comprehensive explanation for their driving mechanism, however, remains elusive. More than twenty years ago, [Chen et al.](#page-8-0) [\(2002\)](#page-8-0) proposed that the broad QFP wave train could be caused by the successive stretching of the magnetic field lines during the eruption of the filament. However, recent research by [Ye et al.](#page-9-37) [\(2021\)](#page-9-37) using a 2.5D MHD simulation suggests that turbulence plays a crucial role in generating the broad QFP wave train around the CME. Furthermore, [Hu et al.](#page-8-17) [\(2024\)](#page-8-17) offers a new perspective on understanding the triggering of broad QFP wave trains. They propose that the leakage of internal disturbances in the magnetic rope acts as a waveguide, forming a multiple wavefront structure as a reasonable mechanism for wave train generation. The case in the current study cannot or is difficult to provide observational evidence for supporting these numerical simulations. [Liu et al.](#page-9-19) [\(2012\)](#page-9-19), first reported the broad QFP wave train, believe that the broad QFP wave train should be driven by the periodic energy release of the associate flare because the wave train shares a common periodic with the flare. This view is supported by the subsequent observational event and numerical simulations; for example, [Zhou et al.](#page-10-8) [\(2022b,](#page-10-8)[c\)](#page-10-1) find these wave trains share a common period with the accompanying flare. In the numerical experiment conducted by [Wang et al.](#page-9-24) [\(2021\)](#page-9-24), a series of wavefronts with a domeshape excited by the energy release associated with the flare. However, in the event reported here, the period of the accompanying flare does not align with that of the broad wave train but is consistent with that of the narrow wave train. Thus, we propose that the flare only excited the narrow QFP wave train. Previous studies have suggested that jets can drive coronal waves in front of them [\(Shen et al.](#page-9-38) [2018a;](#page-9-38) [Duan et al.](#page-8-18) [2022\)](#page-8-18), equivalent to the piston-driven scenario in a shock tube: once the shock wave detaches with the piston (jet), it can continue propagation freely [\(Lulic et al.](#page-9-39) 2013). Particularly, [Shen et al.](#page-9-38) $(2018a)$ identified four homologous EUV waves originating from the same active region. The findings indicate that those recurrent waves were driven by the recurrent jets. In contrast to the that scenario, the jet in the present case did not erupt intermittently; instead, it exhibited a pronounced periodic rotational motion during its eruption. By tracking a bright feature moving helically in the jet, we find that its unwinding period is about 120 s. This period is consistent with that of the broad QFP wave train. On the other hand, the onset time of the narrow QFP wave train and flare QPPs was essentially the same, occurring at 8:46 UT (see the animation of Figure [3\)](#page-7-3). However, the initiation time of the broad QFP wave train was approximately $08:44$ UT (refer to the red arrow in Figure $4(a2)$ $4(a2)$), coinciding

Figure 1. Panel (a) shows the initial coronal condition of the eruption source region using the SDO/AIA 171 Å raw image, where the green curve lines overlying the filament are the extrapolated open magnetic-field lines obtained using the PFSS model. Panels (b)-(i) display the evolution of the jet with the SDO/AIA 304 Å and 131 Å raw image. The white lines marked S1-S5 in panel (c) represent the positions to obtain time-distance stack plots to trace the evolution of the jet in perpendicular and parallel directions to the jet's central axis. Two perpendicular coordinate axes labeled with x' and y' overlaid in panel (g) are used as a coordinate system to trance the moving bright features, which are also plotted in Figure [2](#page-6-0) (a1). An animation of this image is available. The animation covers 08:35 UT-08:55 UT with a 12 s cadence. The animation is 3 s.

with the interaction between the unwinding structures of the jet and the solar surface (refer to the red arrow in Figure [2\(](#page-6-0)b1)) but preceding the narrow QFP wave train and flare by approximately 2 minutes. Based on this temporal and period relationship, we propose that the broad QFP wave train should not be triggered by the flare QPPs, but is the jet's rotation motion. The jet' unwinding is also one type of periodic energy release of the magnetic twist stored in the filament into the outer corona [\(Shibata](#page-9-40) [& Uchida](#page-9-40) [1986;](#page-9-40) [Canfield et al.](#page-7-4) [1996;](#page-7-4) [Hong et al.](#page-8-19) [2013\)](#page-8-19). The reported broad QFP here is potentially formed as a result of the untwisting of the filament via jet. Jets involving filament eruptions are generally called blowout jets [\(Moore et al.](#page-9-41) [2010;](#page-9-41) [Sterling](#page-9-42) [et al.](#page-9-42) [2015\)](#page-9-42) or breakout jets [\(Wyper et al.](#page-9-43) [2017\)](#page-9-43) in historical literature. No matter in which jet model, as the filament in the jet base continuously ascends, interchange reconnection between the ambient field and filament is expected to occur. Once such interchange reconnection occurs, the twist of the filament ultimately would relax into the ambient field and form the unwinding jet [\(Shen et al.](#page-9-44) [2011;](#page-9-44) [Canfield et al.](#page-7-4) [1996;](#page-7-4) [Pariat et al.](#page-9-45) [2009;](#page-9-45) [Yang et al.](#page-9-46) [2023,](#page-9-46) [2024\)](#page-9-47).

We find that many jets with highly rotational motion are not accompanied by broad QFP wave train, such as the jets reported by [Shen et al.](#page-9-44) [\(2011\)](#page-9-44), [Hong et al.](#page-8-19) [\(2013\)](#page-8-19), [Li & Zhang](#page-9-48) [\(2015\)](#page-9-48) and [Chen et al.](#page-7-1) [\(2021\)](#page-7-1). We speculate that it may be due to the

Figure 2. Panel (a1) shows the coordinate system $x' - y'$ relative to the arcsec coordinate system $x - y$. The color "+" symbols in the inset of panel (a1) represent the variations of the location coordinates of the moving bright features relative to the $x' - y'$ coordinate system. Panels (a2) and (a3) show the evolution of moving bright features in the *x'*- and *y'*-directions, respectively. The fitted parameters are list on the corresponding panels. Panels (b1) -(d) are the time-distance stack plots reconstructed along the slices S1-S5 in Figure [1,](#page-5-0) using the AIA 131 Å (b1-b4) and 304 Å (c1-d) raw images. The ridges' slope represents the moving material's speeds, and their speeds obtained by linear fitting are listed in each panel. Errors in parameters such as speed, period, etc are estimated by making the fit ten times.

incline angle of the jet's axis relative to the solar surface being too large; for example, the jets reported by [Shen et al.](#page-9-44) [\(2011\)](#page-9-44) and [Hong et al.](#page-8-19) [\(2013\)](#page-8-19), they were almost near to 90°. We can get inspiration from Zheng's research result for the explanation of the origin of the Moreton wave in the Chromosphere [\(Zheng et al.](#page-10-15) [2023\)](#page-10-15): only when the direction of the eruption is incline enough relative to the solar surface can it cause effectively disturb the solar corona. This can be verified by the appearance position of the wave signal which is only in the southward direction consistent with the jet inclination in the current event. We hypothesize that, apart from the incline angle, the expansion occurring during jet untwisting could also be a crucial factor in initiating the broad QFP wave train in the current event because it can facilitate the efficient release of stored magnetic twist energy.

Studying the coronal waves is of particular importance in solar physics since they play an essential role in coronal heating [\(Long et al.](#page-9-49) [2019;](#page-9-49) [Zhou et al.](#page-10-6) [2022a\)](#page-10-6), diagnosing the magnetic field strength [\(Uchida](#page-9-0) [1970;](#page-9-0) [Roberts et al.](#page-9-1) [1984\)](#page-9-1) and detected the information inside the coronal hole using the lensing effect [\(Zhou et al.](#page-10-0) [2024b\)](#page-10-0). The single impulsive lateral expansion of the CME, an explanation for the driven mechanism of the classical large-scale coronal wave, is not adapted to explain the origin of these broad waves characterized by multiple wavefronts. Consequently, We anticipate that a unified explanation of the QFP wave train will materialize in the future. Of course, it is also possible that triggering mechanisms itself is diverse. As the Sun enters the solar cycle 25, the sun is reaching its maximum [\(Chen](#page-8-20) [2023b\)](#page-8-20). This is conducive to combining the observation by SDO and new solar observatories recently launched by China, such as ASO-S [\(Gan et al.](#page-8-21) [2019,](#page-8-21) [2023\)](#page-8-22), CHASE [\(Li et al.](#page-8-23) [2022\)](#page-8-23) and SUTRI [\(Bai et al.](#page-7-5) [2023\)](#page-7-5), to carry out more comprehensive study on the trigger mechanism of the QFP wave trains, especially, the broad QFP wave train.

4. ACKNOWLEDGMENTS

We want to thank the anonymous referees for the many valuable suggestions and comments for improving the quality of this paper, and we are thankful to the teams of SDO and GOES for providing excellent data. This work is supported by the Natural Science Foundation of China (12303062), the Sichuan Science and Technology Program (2023NSFSC1351), and the Project Supported by the Specialized Research Fund for State Key Laboratories. Y.D.S is supported by the Natural Science Foundation of China (12173083) and the Yunnan Science Foundation for Distinguished Young Scholars (202101AV070004). Coauthor

AIA 171Å 08:46:48UT AIA 171Å 08:47:00UT AIA 171Å 08:47:48UT (b) (c) AIA 211Å 08:50:36UT (d) AIA 171Å 08:46:48UT (e) AIA 193Å 08:50:31UT (f) Open-loops (arcsec) 1100 1200 1000 800

Figure 3. The running-difference images in SDO/AIA 171 Å, 193 Å and 211 Å show the snapshots of the wave train at different times, in which the green and red arrows indicate the wavefronts of the narrow and broad QFP wave trains, respectively. Meanwhile, the wavefronts of the broad QFP are also highlighted by the green curve in panels (a)-(c) and (e)-(f). The rectangles marked Sa and Sb overlaid on the SDO/AIA 171 Å raw image are used to reconstruct the time-distance plots in Figure [4,](#page-8-10) while the white dotted line sketch the boundary of the open-loops system. An animation of this image is available. The animation covers 08:35 UT-9:05 UT with a 12 s cadence. The animation is 5 s.

A.A.I would like to thank the Researchers Supporting Project (Grant No. RSPD2024R993), King Saud University, Riyadh, Saudi Arabia. We gratefully acknowledge ISSI-BJ for supporting the international team "Magnetohydrodynamic wave trains as a tool for probing the solar corona". We also acknowledge Sichuan Normal University Astrophysical Laboratory Supercomputer for providing providing the computational resources. The Wavelet^{[2](#page-7-6)} software was provided by C. Torrence and G. Compo.

REFERENCES

Antolin, P., Pagano, P., Testa, P., Petralia, A., & Reale, F. 2021, Nature Astronomy, 5, 54, doi: 10.1038/[s41550-020-1199-8](http://doi.org/10.1038/s41550-020-1199-8) Bai, X., Tian, H., Deng, Y., et al. 2023, RAA, 23, 065014, doi: 10.1088/[1674-4527](http://doi.org/10.1088/1674-4527/accc74)/accc74

² https://[paos.colorado.edu](https://paos.colorado.edu/research/wavelets/)/research/wavelets/

Canfield, R. C., Reardon, K. P., Leka, K. D., et al. 1996, ApJ, 464, 1016, doi: [10.1086](http://doi.org/10.1086/177389)/177389

Chandra, R., Chen, P. F., Joshi, R., Joshi, B., & Schmieder, B. 2018, ApJ, 863, 101, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aad097)/aad097

Chen, H., Yang, J., Hong, J., Li, H., & Duan, Y. 2021, ApJ, 911, 33, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/abe6a8)/abe6a8

Figure 4. Panels (a1)-(a3) are the time-distance stack plots obtained from the AIA 171 Å and 193 Å running-difference images along the slice Sa and Sb shown in Figure [3](#page-7-3) (d). The white arrows in panels (a2) point to the positions where the intensity profile is used to analyze the periodicity of the wave trains. Panel (b1) display the GOES 1-8 \AA X-ray flux and normalized AIA 94 \AA , 131 \AA and 335 \AA light flux curves within the eruption source region marked with the black box in Figure [1](#page-5-0) (i). Panel (b2) is the derivative curve of the GOES 1-8 \AA flux. Panel (c1) and (c2) respectively show the wavelet spectrum of the flare and broad QFP wave train, and their corresponding periods are listed in the figures. The main periods and their errors are determined by the peak and full width at half maximum (FWHM) of the corresponding global wavelet power spectra. The dark blue curves in wavelet spectrum outline the 95% significance level, while the cross-hatched areas in wavelet spectrum indicate the cone of influence region due to the edge effect of the data. Panels (d1)-(d3) are three snapshots to show the evolution of the narrow QFP wave train, where the red arrow in each panel is located at a specific position.

- Chen, P. F. 2016, GMS, 216, 381,
- doi: 10.1002/[9781119055006.ch22](http://doi.org/10.1002/9781119055006.ch22)
- —. 2023a, Rev. Geophys. Planet. Phys., 54, 355, doi: 10.19975/[j.dqyxx.2022-066](http://doi.org/10.19975/j.dqyxx.2022-066)
- —. 2023b, SCPMA, 66, 129631, doi: 10.1007/[s11433-023-2228-8](http://doi.org/10.1007/s11433-023-2228-8)
- Chen, P. F., Wu, S. T., Shibata, K., & Fang, C. 2002, ApJL, 572, L99, doi: [10.1086](http://doi.org/10.1086/341486)/341486
- Duan, Y., Shen, Y., Zhou, X., et al. 2022, ApJL, 926, L39, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ac4df2)/ac4df2
- Gan, W., Zhu, C., Deng, Y., et al. 2023, SoPh, 298, 68, doi: 10.1007/[s11207-023-02166-x](http://doi.org/10.1007/s11207-023-02166-x)
- Gan, W.-Q., Zhu, C., Deng, Y.-Y., et al. 2019, RAA, 19, 156, doi: 10.1088/[1674-4527](http://doi.org/10.1088/1674-4527/19/11/156)/19/11/156
- Hong, J.-C., Jiang, Y.-C., Yang, J.-Y., et al. 2013, RAA, 13, 253, doi: 10.1088/[1674-4527](http://doi.org/10.1088/1674-4527/13/3/001)/13/3/001
- Hou, Z., Tian, H., Su, W., et al. 2023, ApJ, 953, 171, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ace31b)/ace31b
- Hou, Z., Tian, H., Wang, J.-S., et al. 2022, ApJ, 928, 98, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ac590d)/ac590d
- Hu, J., Ye, J., Chen, Y., et al. 2024, ApJ, 962, 42, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ad1993)/ad1993
- Kumar, P., Innes, D. E., & Cho, K.-S. 2016, ApJ, 828, 28, doi: 10.3847/[0004-637X](http://doi.org/10.3847/0004-637X/828/1/28)/828/1/28
- Kumar, P., Nakariakov, V. M., & Cho, K.-S. 2017, ApJ, 844, 149, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aa7d53)/aa7d53
- Kumar, P., Nakariakov, V. M., Karpen, J. T., & Cho, K.-S. 2024, NatCo, 15, 2667, doi: 10.1038/[s41467-024-46736-4](http://doi.org/10.1038/s41467-024-46736-4)
- Kupriyanova, E. G., Melnikov, V. F., & Shibasaki, K. 2013, SoPh, 284, 559, doi: 10.1007/[s11207-012-0141-3](http://doi.org/10.1007/s11207-012-0141-3)
- Lemen, J. R., Title, A. M., Akin, D. J., et al. 2012, SoPh, 275, 17, doi: 10.1007/[s11207-011-9776-8](http://doi.org/10.1007/s11207-011-9776-8)
- Li, C., Fang, C., Li, Z., et al. 2022, SCPMA, 65, 289602, doi: 10.1007/[s11433-022-1893-3](http://doi.org/10.1007/s11433-022-1893-3)
- Li, D., & Chen, W. 2022, ApJL, 931, L28, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ac6fd2)/ac6fd2
- Li, D., Dong, H., Chen, W., et al. 2024a, SoPh, 299, 57, doi: 10.1007/[s11207-024-02299-7](http://doi.org/10.1007/s11207-024-02299-7)
- Li, D., Feng, S., Su, W., & Huang, Y. 2020a, A&A, 639, L5, doi: 10.1051/0004-6361/[202038398](http://doi.org/10.1051/0004-6361/202038398)
- Li, D., Hong, Z., Hou, Z., & Su, Y. 2024b, ApJ, 970, 77, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ad566c)/ad566c
- Li, D., Hou, Z., Bai, X., et al. 2024c, Science in China E: Technological Sciences, 67, 1592, doi: 10.1007/[s11431-023-2534-8](http://doi.org/10.1007/s11431-023-2534-8)
- Li, D., Li, Y., Lu, L., et al. 2020b, ApJL, 893, L17, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ab830c)/ab830c
- Li, D., Lu, L., Ning, Z., et al. 2020c, ApJ, 893, 7, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ab7cd1)/ab7cd1
- Li, D., & Zhang, Q. M. 2017, MNRAS, 471, L6, doi: [10.1093](http://doi.org/10.1093/mnrasl/slx091)/mnrasl/slx091
- Li, D., Ge, M., Dominique, M., et al. 2021, ApJ, 921, 179, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ac1c05)/ac1c05
- Li, L., Zhang, J., Peter, H., et al. 2018, ApJL, 868, L33, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/aaf167)/aaf167
- Li, T., & Zhang, J. 2015, SoPh, 290, 2857, doi: 10.1007/[s11207-015-0768-y](http://doi.org/10.1007/s11207-015-0768-y)
- Li, T., Zhang, J., Yang, S., & Liu, W. 2012, ApJ, 746, 13, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/746/1/13)/746/1/13
- Liu, R., Wang, Y., Lee, J., & Shen, C. 2019, ApJ, 870, 15, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aaf04e)/aaf04e
- Liu, W., Jin, M., Downs, C., et al. 2018, ApJL, 864, L24, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/aad77b)/aad77b
- Liu, W., & Ofman, L. 2014, SoPh, 289, 3233, doi: 10.1007/[s11207-014-0528-4](http://doi.org/10.1007/s11207-014-0528-4)
- Liu, W., Ofman, L., Nitta, N. V., et al. 2012, ApJ, 753, 52, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/753/1/52)/753/1/52
- Liu, W., Title, A. M., Zhao, J., et al. 2011, ApJL, 736, L13, doi: 10.1088/[2041-8205](http://doi.org/10.1088/2041-8205/736/1/L13)/736/1/L13
- Liu, Y., Zheng, R., Zhang, L., et al. 2023, A&A, 674, A167, doi: 10.1051/0004-6361/[202345836](http://doi.org/10.1051/0004-6361/202345836)
- Long, D. M., Jenkins, J., & Valori, G. 2019, ApJ, 882, 90, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ab338d)/ab338d
- Lulić, S., Vršnak, B., Žic, T., et al. 2013, SoPh, 286, 509, doi: 10.1007/[s11207-013-0287-7](http://doi.org/10.1007/s11207-013-0287-7)
- Ma, S., Raymond, J. C., Golub, L., et al. 2011, ApJ, 738, 160, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/738/2/160)/738/2/160
- Mei, Z. X., Keppens, R., Cai, Q. W., et al. 2020, MNRAS, 493, 4816, doi: [10.1093](http://doi.org/10.1093/mnras/staa555)/mnras/staa555
- Miao, Y., Li, D., Yuan, D., et al. 2021, ApJL, 908, L37, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/abdfce)/abdfce
- Moore, R. L., Cirtain, J. W., Sterling, A. C., & Falconer, D. A. 2010, ApJ, 720, 757, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/720/1/757)/720/1/757
- Nakariakov, V. M., & Melnikov, V. F. 2009, SSRv, 149, 119, doi: 10.1007/[s11214-009-9536-3](http://doi.org/10.1007/s11214-009-9536-3)
- Nakariakov, V. M., & Stepanov, A. V. 2007, in Lecture Notes in Physics, Berlin Springer Verlag, ed. K.-L. Klein & A. L. MacKinnon, Vol. 725, 221
- Neupert, W. M. 1968, ApJL, 153, L59, doi: [10.1086](http://doi.org/10.1086/180220)/180220
- Nitta, N. V., Schrijver, C. J., Title, A. M., & Liu, W. 2013, ApJ, 776, 58, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/776/1/58)/776/1/58
- Pariat, E., Antiochos, S. K., & DeVore, C. R. 2009, ApJ, 691, 61, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/691/1/61)/691/1/61
- Pesnell, W. D., Thompson, B. J., & Chamberlin, P. C. 2012, SoPh, 275, 3, doi: 10.1007/[s11207-011-9841-3](http://doi.org/10.1007/s11207-011-9841-3)
- Piantschitsch, I., & Terradas, J. 2021, A&A, 651, A67, doi: 10.1051/0004-6361/[202040182](http://doi.org/10.1051/0004-6361/202040182)
- Roberts, B., Edwin, P. M., & Benz, A. O. 1984, ApJ, 279, 857, doi: [10.1086](http://doi.org/10.1086/161956)/161956 Schrijver, C. J., & De Rosa, M. L. 2003, SoPh, 212, 165, doi: 10.1023/[A:1022908504100](http://doi.org/10.1023/A:1022908504100) Shen, Y., Chen, P. F., Liu, Y. D., et al. 2019, ApJ, 873, 22, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ab01dd)/ab01dd Shen, Y., & Liu, Y. 2012, ApJ, 753, 53, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/753/1/53)/753/1/53 Shen, Y., Liu, Y., Liu, Y. D., et al. 2018a, ApJ, 861, 105, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aac9be)/aac9be Shen, Y., Liu, Y., Su, J., & Ibrahim, A. 2011, ApJL, 735, L43, doi: 10.1088/[2041-8205](http://doi.org/10.1088/2041-8205/735/2/L43)/735/2/L43 Shen, Y., Liu, Y., Tian, Z., & Qu, Z. 2017, ApJ, 851, 101, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aa9af0)/aa9af0 Shen, Y., Song, T., & Liu, Y. 2018b, MNRAS, 477, L6, doi: [10.1093](http://doi.org/10.1093/mnrasl/sly044)/mnrasl/sly044 Shen, Y., Tang, Z., Li, H., & Liu, Y. 2018c, MNRAS, 480, L63, doi: [10.1093](http://doi.org/10.1093/mnrasl/sly127)/mnrasl/sly127 Shen, Y., Tang, Z., Miao, Y., Su, J., & Liu, Y. 2018d, ApJL, 860, L8, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/aac8dd)/aac8dd Shen, Y., Zhou, X., Duan, Y., et al. 2022, SoPh, 297, 20, doi: 10.1007/[s11207-022-01953-2](http://doi.org/10.1007/s11207-022-01953-2) Shibata, K., & Uchida, Y. 1986, SoPh, 103, 299, doi: 10.1007/[BF00147831](http://doi.org/10.1007/BF00147831) Sterling, A. C., Moore, R. L., Falconer, D. A., & Adams, M. 2015, Nature, 523, 437, doi: 10.1038/[nature14556](http://doi.org/10.1038/nature14556) Su, W., Cheng, X., Ding, M. D., Chen, P. F., & Sun, J. Q. 2015, ApJ, 804, 88, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/804/2/88)/804/2/88 Sun, Z., Tian, H., Chen, P. F., et al. 2022, ApJL, 939, 1, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ac9aff)/ac9aff Thompson, B. J., Plunkett, S. P., Gurman, J. B., et al. 1998, Geophys. Res. Lett., 25, 2465, doi: 10.1029/[98GL50429](http://doi.org/10.1029/98GL50429) Torrence, C., & Compo, G. P. 1998, Bulletin of the American Meteorological Society, 79, 61, doi: 10.1175/[1520-0477\(1998\)079](http://doi.org/10.1175/1520-0477(1998)079<0061:APGTWA>2.0.CO;2)⟨0061:APGTWA⟩2.0.CO;2 Uchida, Y. 1970, PASJ, 22, 341 Wang, C., Chen, F., & Ding, M. 2021, ApJL, 911, L8, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/abefe6)/abefe6 Warmuth, A. 2015, Living Reviews in Solar Physics, 12, 3, doi: 10.1007/[lrsp-2015-3](http://doi.org/10.1007/lrsp-2015-3) Wu, S. T., Zheng, H., Wang, S., et al. 2001, J. Geophys. Res., 106, 25089, doi: 10.1029/[2000JA000447](http://doi.org/10.1029/2000JA000447) Wyper, P. F., Antiochos, S. K., & DeVore, C. R. 2017, Nature, 544, 452, doi: 10.1038/[nature22050](http://doi.org/10.1038/nature22050) Yang, J., Chen, H., Hong, J., Yang, B., & Bi, Y. 2024, ApJ, 964, 7, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ad23e5)/ad23e5 Yang, J., Hong, J., Yang, B., Bi, Y., & Xu, Z. 2023, ApJ, 942, 86, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aca66f)/aca66f Ye, J., Cai, Q., Shen, C., et al. 2021, ApJ, 909, 45, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/abdeb5)/abdeb5
- Yuan, D., Shen, Y., Liu, Y., et al. 2013, A&A, 554, A144, doi: 10.1051/0004-6361/[201321435](http://doi.org/10.1051/0004-6361/201321435)
- Zhang, Q. 2024, Reviews of Modern Plasma Physics, 8, 7, doi: 10.1007/[s41614-024-00144-9](http://doi.org/10.1007/s41614-024-00144-9)
- Zhang, Q., Li, C., Li, D., et al. 2022, ApJL, 937, L21, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ac8e01)/ac8e01
- Zhang, Q. M., Li, D., & Ning, Z. J. 2016, ApJ, 832, 65, doi: 10.3847/[0004-637X](http://doi.org/10.3847/0004-637X/832/1/65)/832/1/65
- Zhang, Y., Zhang, J., Wang, J., & Nakariakov, V. M. 2015, A&A, 581, A78, doi: 10.1051/0004-6361/[201525621](http://doi.org/10.1051/0004-6361/201525621)
- Zheng, R., Chen, Y., Wang, B., & Song, H. 2020, ApJ, 894, 139, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ab863c)/ab863c
- Zheng, R., Jiang, Y., Yang, J., et al. 2012, A&A, 541, A49, doi: 10.1051/0004-6361/[201118305](http://doi.org/10.1051/0004-6361/201118305)
- —. 2013, ApJ, 764, 70, doi: 10.1088/[0004-637X](http://doi.org/10.1088/0004-637X/764/1/70)/764/1/70
- Zheng, R., Liu, Y., Liu, W., et al. 2023, ApJL, 949, L8, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/acd0ac)/acd0ac
- Zhou, X., Shen, Y., Liang, H., et al. 2022a, ApJ, 941, 59, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/aca1b6)/aca1b6
- Zhou, X., Shen, Y., Su, J., et al. 2021, SoPh, 296, 169, doi: 10.1007/[s11207-021-01913-2](http://doi.org/10.1007/s11207-021-01913-2)
- Zhou, X., Shen, Y., Tang, Z., et al. 2022b, A&A, 659, A164, doi: 10.1051/0004-6361/[202142536](http://doi.org/10.1051/0004-6361/202142536)
- Zhou, X., Shen, Y., Zhou, C., Tang, Z., & Ibrahim, A. A. 2024a, SCPMA, 67, 259611, doi: 10.1007/[s11433-023-2309-5](http://doi.org/10.1007/s11433-023-2309-5)
- Zhou, X., Shen, Y., Liu, Y. D., et al. 2022c, ApJL, 930, L5, doi: 10.3847/[2041-8213](http://doi.org/10.3847/2041-8213/ac651e)/ac651e
- Zhou, X., Shen, Y., Yuan, D., et al. 2024b, NatCo, 15, 3281, doi: 10.1038/[s41467-024-46846-z](http://doi.org/10.1038/s41467-024-46846-z)
- Zhou, X., Shen, Y., Yan, Y., et al. 2024c, ApJ, 968, 85, doi: 10.3847/[1538-4357](http://doi.org/10.3847/1538-4357/ad4456)/ad4456